

AREA OF COMPOUND SHAPES REAL LIFE EXAMPLES Tutorial

area of compound shapes real life examples is a fascinating topic that bridges the gap between mathematical concepts and everyday practical applications. Understanding how to calculate the area of compound shapes is essential not only in academic settings but also in various industries and real-world scenarios. From architecture and interior design to engineering and landscaping, the ability to determine the space occupied by complex shapes plays a crucial role in planning, resource management, and cost estimation. This article explores numerous real-life examples of compound shapes, demonstrates how to calculate their areas, and highlights the importance of these calculations across different fields.

Understanding Compound Shapes

Before delving into real-life examples, it's vital to grasp what compound shapes are. A compound shape, also known as a composite shape, is a figure made up of two or more simple geometric shapes such as rectangles, squares, triangles, circles, or semi-circles. These shapes are combined in various ways to create more complex figures.

Key Points about Compound Shapes

- They often consist of overlapping or adjoining simple shapes.
- Calculating their area involves dividing the compound shape into simpler parts.
- The total area is usually found by summing the areas of individual shapes, subtracting overlaps, or adding areas of disjoint shapes.

Real-Life Examples of Compound Shapes

1. Architectural Floor Plans

Architects frequently design building layouts that are complex in shape. Many modern homes and commercial buildings feature floor plans that combine rectangles, squares, and semi-circular sections.

- **Example:** A house plan might include a rectangular main living area with a semi-circular porch attached on one side. Calculating the total floor space involves finding the area of the rectangle and

the semi-circle separately, then adding them together.

- **Importance:** Precise area calculation helps determine the amount of flooring material needed and the overall space available for furnishing and movement.

2. Land Parcel Measurement in Agriculture and Real Estate

Farmers and real estate developers often deal with irregularly shaped plots of land. These plots can be modeled as compound shapes made up of rectangles, triangles, and circles.

- **Example:** A farm plot might include a rectangular section for crops, a triangular corner for a water reservoir, and a circular pond. Calculating the total area requires breaking down the plot into these simple shapes, calculating each area, and summing them up.

- **Importance:** Accurate measurement ensures fair land valuation, proper resource allocation, and effective land use planning.

3. Interior Design and Space Planning

Interior designers often work with rooms that are not perfect rectangles, incorporating curved walls or semi-circular alcoves.

- **Example:** Designing a living room with a rectangular main space and a semi-circular bay window area involves calculating the area of both parts separately.

- **Importance:** Knowing the exact area helps in selecting the right amount of paint, wallpaper, or flooring material, leading to cost efficiency.

4. Sports Fields and Recreation Areas

Many sports fields are designed with composite shapes to maximize space and functionality.

- **Example:** A football field with rounded ends (semi-circular) and rectangular central areas is a common compound shape. Calculating the total area is essential for compliance with regulations and for setting up boundary markers.

- **Importance:** Precise area measurement ensures proper field layout and adherence to official standards.

5. Engineering and Manufacturing

Manufacturers often produce parts with complex shapes, which need precise area calculations for

material estimation and quality control.

- **Example:** A car hood design might include a rectangular base with semi-circular protrusions. Calculating the surface area is crucial for coating and finishing processes.

- **Importance:** Accurate area measurements optimize material use, reduce waste, and improve product quality.

How to Calculate the Area of Compound Shapes

Calculating the area of a compound shape involves several steps:

Step-by-Step Process

- Identify the individual shapes: Break down the complex figure into basic shapes such as rectangles, triangles, circles, etc.
- Calculate the area of each shape: Use standard formulas for each shape.
- Determine overlaps and gaps: If shapes overlap, subtract the overlapping area to avoid double counting.
- Sum the areas: Add the areas of all individual shapes, accounting for overlaps or gaps.
- Verify: Cross-check calculations to ensure accuracy.

Formulas for Common Shapes

- Rectangle: $\text{Area} = \text{length} \times \text{width}$
- Square: $\text{Area} = \text{side} \times \text{side}$
- Triangle: $\text{Area} = \frac{1}{2} \times \text{base} \times \text{height}$
- Circle: $\text{Area} = \pi \times \text{radius}^2$
- Semi-circle: $\text{Area} = \left(\frac{1}{2}\right) \times \pi \times \text{radius}^2$

Practical Tips for Calculating Areas of Compound Shapes

- Use graph paper or digital drawing tools to visualize and divide the shape.
- Keep track of units to ensure consistency.
- Use calculators or software for complex calculations.
- When shapes are overlapping or irregular, approximate using irregular polygons or digital tools.

Benefits of Understanding Areas of Compound Shapes in Real Life

- Cost estimation: Accurate area calculations help estimate costs for materials such as paint, flooring, or land development.
- Design efficiency: Optimizing space usage in architecture and interior design.
- Resource management: Proper allocation of resources based on precise measurements.
- Legal and regulatory compliance: Ensuring that land and property measurements meet legal standards.
- Environmental planning: Calculating green space, water bodies, and recreational areas.

Conclusion

The concept of the area of compound shapes extends far beyond classroom exercises, playing a vital role in numerous real-world applications. From designing functional living spaces and measuring land to manufacturing complex parts, understanding how to calculate and work with composite shapes enhances efficiency, accuracy, and resource management. Whether you are an architect, engineer, farmer, or hobbyist, mastering the principles of compound shape area calculation empowers you to make informed decisions and optimize your projects effectively. Embrace these skills to navigate the complexities of real-world shapes and unlock their full potential in practical scenarios.

Area of Compound Shapes Real Life Examples

Understanding the concept of the area of compound shapes is essential not only in academic settings but also in everyday life. Many real-world objects and structures are composed of multiple basic geometric shapes combined to form complex figures. Accurately calculating the area of these compound shapes allows architects, engineers, designers, and homeowners to make informed decisions, optimize space, and ensure efficient resource usage. This article explores various real-life examples of compound shapes, illustrating how their area calculations are applied across different fields.

What Are Compound Shapes?

Before diving into real-life examples, it's important to clarify what compound shapes are. A compound shape is a figure formed by combining two or more simple geometric shapes such as rectangles, triangles, circles, or trapezoids. These shapes can be joined edge-to-edge or overlapping, creating a complex figure that requires breaking down into simpler parts to calculate its total area accurately.

Calculating the area of a compound shape typically involves:

- Dividing the shape into simpler components.

- Calculating the area of each component separately.
- Adding or subtracting the areas depending on the shape's structure.

This systematic approach simplifies complex calculations, making it easier to analyze real-world problems involving irregular or composite figures.

Real-Life Examples of Compound Shapes

- Land Plotting and Property Boundaries

Scenario: Imagine a homeowner planning to build a garden within their backyard, which is not a perfect rectangle. Instead, the yard comprises a rectangular section with a semicircular extension on one side.

Application:

In this case, the total area of the backyard can be calculated by dividing the figure into:

- A rectangle representing the main yard.
- A semicircle attached to one side for the garden extension.

Calculation:

- Rectangle area: $\text{Length} \times \text{Width}$.
- Semicircular area: $(\frac{1}{2}) \times \pi \times r^2$, where r is the radius of the semicircle.

Importance: Knowing the total area allows the homeowner to estimate the amount of soil, grass, or paving needed, as well as to plan for fencing or landscaping.

- Architecture and Building Design

Scenario: An architect designing a new community center needs to determine the floor area of a complex-shaped hall. The hall's layout includes a rectangular main area with an attached circular lobby.

Application:

- The main hall: a rectangle.
- The lobby: a sector of a circle or a full circle, depending on design.

Calculation:

- Rectangular part: length $\times$ width.
- Circular lobby: $\frac{\theta}{360} \times \pi r^2$ (full circle) or a fraction thereof (sector).

Real-Life Impact: Accurate area calculations influence material estimates (like flooring and wall paint), HVAC planning, and budget estimates. Additionally, knowing the precise area helps in complying with building codes and regulations.

- Road and Pathway Planning

Scenario: City planners need to determine the surface area of a new park pathway that combines straight and curved segments. The pathway includes a rectangular straight path with a semicircular turnaround at the end.

Application:

- Rectangular segment: straightforward length $\times$ width.
- Semicircular turnaround: $\frac{1}{2} \times \pi r^2$.

Usage:

This calculation guides the procurement of paving materials and helps in estimating the time and labor required for construction.

- Decorative Items and Art Installations

Scenario: An artist designing a large decorative mosaic that combines rectangular and circular tiles into a single piece.

Application:

- Calculating the total mosaic area involves summing the areas of individual tiles, some

rectangular and some circular.

- Ensuring the total surface coverage is sufficient and estimating the amount of tiles needed.

Broader Impact: Precise area measurement informs material purchase, cost estimation, and logistical planning.

- Agricultural Field Planning

Scenario: A farmer has a field that is partly rectangular and partly circular (e.g., a circular pond within the farm). To optimize planting and irrigation, they need to calculate the total cultivable area.

Application:

- The rectangular part: $\text{length} \times \text{width}$.
- The circular part: $\pi \times r^2$.

Significance: Efficient land use planning depends on accurate area calculations, which influence crop selection, fertilizer application, and machinery deployment.

Methods for Calculating the Area of Compound Shapes

When faced with complex figures, the key is to break down the shape into manageable parts:

Step 1: Identify Simple Shapes

- Recognize the basic shapes that compose the compound figure.
- Note overlapping areas or cutouts that need to be subtracted.

Step 2: Divide the Shape

- Sketch the shape and draw lines to divide it into simpler components.
- Use symmetry or existing features to guide division.

Step 3: Calculate Individual Areas

- Use standard formulas for rectangles, triangles, circles, trapezoids, etc.

- For irregular shapes, approximate by dividing into multiple simple shapes.

Step 4: Adjust for Overlaps or Subtractions

- If parts overlap or are cut out, subtract the areas accordingly.
- Ensure all parts are accounted for without double counting.

Step 5: Sum or Subtract Areas

- Add the areas of all positive components.
- Subtract the areas of any cutouts or overlaps.

Practical Tips for Accurate Calculations

- Use precise measurements: Always measure lengths and radii accurately.
- Convert units consistently: Keep all measurements in the same units before calculating.
- Use calculator or software: For complex shapes, CAD software or online calculators can enhance precision.
- Double-check divisions: Ensure the shape is divided correctly, especially when dealing with overlapping parts.
- Estimate and verify: Cross-verify calculations with estimations to prevent errors.

Significance of Area Calculations in Various Fields

The ability to accurately calculate the area of compound shapes is pivotal in numerous disciplines:

- Construction: Ensuring structures are built within spatial constraints.
- Landscaping: Optimizing space utilization and aesthetic appeal.
- Manufacturing: Cutting materials efficiently to reduce waste.
- Urban Planning: Designing functional and sustainable public spaces.
- Interior Design: Planning furniture layout and floor coverings.

In each case, precise area measurements lead to cost savings, resource efficiency, and better project outcomes.

Conclusion

The area of compound shapes transcends theoretical mathematics, permeating many aspects of daily life and professional practice. From designing a garden to planning a city park, the ability to analyze and compute the area of complex figures is invaluable. Recognizing how different simple shapes combine to form more intricate structures enables us to solve practical problems with confidence and accuracy. As technology advances, tools like CAD software further simplify these calculations, but understanding the fundamental principles remains essential for making informed decisions and ensuring the success of projects across diverse fields.

By mastering the calculation of areas of compound shapes, individuals and professionals alike can better interpret spatial information, optimize resource use, and bring their visions to life efficiently and effectively.

Question How is the area of a composite garden with a circular flower bed and rectangular lawn calculated? The total area is found by calculating the area of each shape separately using πr^2 for the circle and $\text{length} \times \text{width}$ for the rectangle and then adding them together. **Answer** How can understanding the area of compound shapes help in designing a custom swimming pool? Knowing how to calculate the area of various sections of the pool, such as a rectangular main area and a semicircular end, helps in estimating materials needed and planning construction efficiently. What is a real-life example of calculating the area of a compound shape in home renovation? When remodeling a room with a rectangular floor and a semicircular bay window area, calculating the total floor space involves summing the areas of both shapes. Why is it important to understand the area of compound shapes in landscaping projects? It helps in estimating the amount of materials like turf, gravel, or paving stones required for different sections of a landscape, which often involve multiple geometric shapes. How do architects use the area of compound shapes in building design? Architects calculate the combined area of complex building sections, such as L-shaped rooms or areas with curved features, to plan space utilization and material estimates. Can calculating the area of compound shapes improve efficiency in manufacturing products? Yes, it helps in estimating material usage for components with complex shapes, reducing waste and optimizing production processes. How is the area of a composite shape relevant in packaging design? Designers calculate the total surface area and base area of packaging with combined shapes to ensure proper fitting, material use, and structural integrity. What tools or formulas are typically used to find the area of compound shapes in real-world applications? The area is usually calculated by dividing the shape into simpler parts, calculating each separately using formulas (like rectangle, triangle, circle), and summing them up. How can understanding the area of compound shapes assist in urban planning? It allows planners to accurately measure land parcels with irregular boundaries, ensuring optimal use of space for parks, roads, and buildings.

Related keywords: compound shapes, real life examples, area calculation, geometry in architecture, land measurement, construction planning, floor design, land surveying, shape analysis, spatial reasoning

word problems area of rectangle square parallelogram

Word problems area of rectangle square parallelogram

Understanding the area of various geometric shapes is fundamental in mathematics, especially when solving real-world problems. Among these shapes, rectangles, squares, and parallelograms are common, and their area calculations form the basis for many word problems encountered in academic and practical settings. Mastering how to approach, interpret, and solve word problems involving these shapes' areas enhances problem-solving skills and mathematical reasoning. This comprehensive guide aims to explore the area concepts for rectangles, squares, and parallelograms through detailed explanations, strategies for solving word problems, and practical examples.

Understanding Basic Concepts of Area

What is Area?

Area refers to the amount of surface covered by a two-dimensional shape. It is measured in square units such as square centimeters (cm²), square meters (m²), or square inches (in²). Calculating the area allows us to determine how much space a shape occupies.

Importance of Area in Real Life

Understanding area calculations helps in various fields such as:

- Architecture and construction (flooring, wall painting)
- Agriculture (farming land measurement)
- Interior design (carpet or tile coverage)
- Art and design (canvas or paper sizes)

Area of Basic Shapes: Rectangles, Squares, and Parallelograms

Rectangle

- Formula: $\text{Area} = \text{length} \times \text{width}$
- Properties: Opposite sides are equal, and angles are right angles.
- Notation: If length = L and width = W, then $\text{Area} = L \times W$.

Square

- Formula: $\text{Area} = \text{side} \times \text{side} = \text{side}^2$
- Properties: All sides are equal, and angles are right angles.
- Note: The square is a special case of a rectangle.

Parallelogram

- Formula: $\text{Area} = \text{base} \times \text{height}$
- Properties: Opposite sides are equal and parallel; angles are not necessarily right angles.
- Note: The height is the perpendicular distance between the bases.

Approach to Solving Word Problems on Area

Solving word problems involving areas requires a systematic approach:

- Read the problem carefully to understand what is given and what is asked.
- Identify the shape involved and recall the relevant formula.
- Extract numerical data and assign variables if needed.
- Determine the missing dimensions (length, width, height, base, etc.).
- Apply the area formula correctly.
- Perform calculations step-by-step.
- Check your answer in the context of the problem.

Strategies for Solving Word Problems

Step-by-Step Problem-Solving Techniques

- Visualize the problem: Draw diagrams or sketches to understand the shape and dimensions.
- Label all given data: Mark known measurements and unknowns clearly.
- Translate words into mathematical expressions: Convert phrases into equations using the formulas.
- Use units consistently: Convert all measurements to the same unit before calculations.
- Estimate before exact calculation: For complex problems, rough estimates can guide your approach.
- Verify the answer: Ensure the solution makes sense logically and contextually.

Common Pitfalls to Avoid

- Confusing perimeter with area.
- Using incorrect formulas for the shape.
- Forgetting to convert units.
- Misreading the problem's data.
- Ignoring the need for perpendicular height in parallelogram problems.

Sample Word Problems and Solutions

Problem 1: Area of a Rectangle

Question: A rectangle has a length of 12 meters and a width of 5 meters. Find its area.

Solution:

- Step 1: Identify given data: Length = 12 m, Width = 5 m.
- Step 2: Recall formula: Area = length $\times$ width.
- Step 3: Calculate: Area = $12 \times 5 = 60 \text{ m}^2$.
- Answer: The rectangle's area is 60 square meters.

Problem 2: Area of a Square

Question: A square garden has a side length of 8 meters. What is the area?

Solution:

- Step 1: Given: Side = 8 m.
- Step 2: Formula: Area = side².
- Step 3: Calculation: $8^2 = 64 \text{ m}^2$.
- Answer: The garden covers 64 square meters.

Problem 3: Area of a Parallelogram

Question: A parallelogram has a base of 15 meters and a height of 6 meters. Find its area.

Solution:

- Step 1: Given: Base = 15 m, Height = 6 m.
- Step 2: Formula: Area = base $\times$ height.

- Step 3: Calculation: $15 \times 6 = 90 \text{ m}^2$.
- Answer: The parallelogram's area is 90 square meters.

Problem 4: Word Problem Combining Shapes

Question: A rectangular park measures 200 meters in length and 150 meters in width. A square playground of side length 30 meters is within the park. Find the area of the remaining part of the park after excluding the playground.

Solution:

- Step 1: Calculate park area: $200 \times 150 = 30,000 \text{ m}^2$.
- Step 2: Calculate playground area: $30^2 = 900 \text{ m}^2$.
- Step 3: Subtract playground area from park area: $30,000 - 900 = 29,100 \text{ m}^2$.
- Answer: The remaining area of the park is 29,100 square meters.

Advanced Word Problems and Applications

Problem 5: Multiple Shapes in a Real-World Context

A farmer has a rectangular field measuring 500 meters by 300 meters. Within it, there is a parallelogram-shaped pond with a base of 100 meters and a height of 40 meters. Find the area of the field that is not occupied by the pond.

Solution:

- Step 1: Calculate total field area: $500 \times 300 = 150,000 \text{ m}^2$.
- Step 2: Calculate pond area: $100 \times 40 = 4,000 \text{ m}^2$.
- Step 3: Subtract pond area from total field: $150,000 - 4,000 = 146,000 \text{ m}^2$.
- Answer: The area of the field excluding the pond is 146,000 square meters.

Problem 6: Applying Area in Construction

A construction company needs to lay tiles on a square kitchen floor of side length 9 meters. If each tile covers 0.25 m^2 , how many tiles are needed to cover the entire floor?

Solution:

- Step 1: Calculate floor area: $9^2 = 81 \text{ m}^2$.
- Step 2: Determine number of tiles: $81 \div 0.25 = 324$ tiles.
- Answer: 324 tiles are required to cover the floor.

Additional Tips for Mastering Word Problems on Area

- Practice regularly: The more problems you solve, the better you understand different scenarios.
- Use diagrams: Visual representation helps in understanding complex problems.
- Understand the context: Real-world problems often contain clues that guide your calculations.
- Check units and conversions: Mistakes often occur due to incorrect units.
- Review formulas: Be sure about the formulas for different shapes and their conditions.

Conclusion

Mastering the area of rectangles, squares, and parallelograms through word problems enhances your mathematical skills and prepares you for tackling real-life situations involving space and measurements. Remember to approach each problem methodically, visualize the shapes involved, and apply the correct formulas. With consistent practice and attention to detail, solving word problems related to the area of these shapes becomes intuitive and rewarding. By understanding these fundamental concepts, you develop a strong foundation for more advanced geometry and problem-solving tasks.

Word Problems in Area of Rectangle, Square, and Parallelogram: A Comprehensive Guide

Understanding how to solve word problems related to the area of rectangles, squares, and parallelograms is a fundamental skill in geometry that combines conceptual understanding with practical problem-solving. These problems are often encountered in academic assessments and real-life scenarios, making mastery in this area essential for students and enthusiasts alike. This comprehensive guide delves into the various aspects of word problems involving the areas of these quadrilaterals, offering detailed explanations, strategies, and examples to enhance your problem-solving toolkit.

Introduction to Area in Quadrilaterals

Before diving into specific word problems, it's crucial to understand what area signifies in the context of rectangles, squares, and parallelograms.

What is Area?

- Definition: Area refers to the amount of surface covered by a two-dimensional shape. It is measured in square units (e.g., square meters, square centimeters).
- Significance: Knowing the area helps in tasks such as flooring, painting, land measurement, and design.

General Formulas

- Rectangle: $\text{Area} = \text{length} \times \text{breadth}$
- Square: $\text{Area} = \text{side}^2$
- Parallelogram: $\text{Area} = \text{base} \times \text{height}$

Note: For parallelograms, the height is perpendicular to the base, which is a key aspect in solving problems.

Understanding Word Problems: Key Concepts and Strategies

Word problems require translating real-world language into mathematical expressions. Here's a structured approach:

Step-by-Step Problem-Solving Strategy

- Read Carefully: Understand what is being asked. Identify the given data and what you need to find.
- Identify the Shape: Recognize whether the problem involves a rectangle, square, or parallelogram.
- Highlight Known Values: Mark the given dimensions, areas, or other relevant information.
- Determine Unknowns: Decide which dimensions or measurements need to be calculated.
- Choose the Correct Formula: Select the appropriate area formula based on the shape.
- Set Up Equations: Translate the problem into mathematical equations.
- Solve the Equations: Perform calculations step-by-step.
- Check Units and Reasonableness: Make sure the units are consistent and the answer makes sense in context.
- Answer in Context: Write the final answer with appropriate units and interpret it if necessary.

Word Problems Involving Rectangles

Rectangles are the most straightforward among these shapes, and their word problems often involve calculating area based on given dimensions or vice versa.

Common Types of Rectangular Area Problems

- Finding the area given length and breadth
- Finding missing dimensions when the area and one dimension are known
- Determining the length or breadth when the area and other dimension are known

Sample Problems and Solutions

Problem 1: A rectangle has a length of 12 meters and a breadth of 5 meters. Find its area.

Solution:

- Use the formula: $\text{Area} = \text{length} \times \text{breadth}$
- $\text{Area} = 12 \times 5 = 60$ square meters

Problem 2: The area of a rectangle is 84 square meters, and its length is 12 meters. Find its breadth.

Solution:

- Rearrange the formula: $\text{breadth} = \frac{\text{Area}}{\text{length}}$
- $\text{breadth} = \frac{84}{12} = 7$ meters

Real-Life Application

- Calculating the area of a garden with given dimensions.
- Determining the amount of material needed for a rectangular tablecloth.

Word Problems Involving Squares

Squares are special rectangles with all sides equal. Their word problems often involve the side length or the area, with the relationship $\text{Area} = \text{side}^2$.

Common Types of Square Area Problems

- Finding area when side length is known

- Finding side length when area is given
- Application in tiling, fencing, and design

Sample Problems and Solutions

Problem 3: The side of a square playground is 20 meters. Find its area.

Solution:

- Use $(\text{Area} = \text{side}^2)$
- $(\text{Area} = 20^2 = 400)$ square meters

Problem 4: A square piece of land has an area of 256 square meters. Find the length of one side.

Solution:

- $(\text{side} = \sqrt{\text{area}})$
- $(\text{side} = \sqrt{256} = 16)$ meters

Practical Applications

- Calculating the amount of paint needed to cover a square wall.
- Determining the size of tiles required for a square floor.

Word Problems Involving Parallelograms

Parallelograms have a more complex area formula involving base and height. Their word problems often include scenarios where height is not directly given, requiring the use of auxiliary data or geometric reasoning.

Common Types of Parallelogram Area Problems

- Calculating area when base and height are known
- Finding missing height or base when the area and other dimensions are given
- Using diagonal and side lengths to find area

Key Concepts for Parallelogram Problems

- The height is perpendicular to the base, not necessarily the side length.
- Sometimes, the problem involves the use of other properties, such as diagonals or angles.

Sample Problems and Solutions

Problem 5: A parallelogram has a base of 15 meters and a height of 8 meters. Find its area.

Solution:

- $\text{Area} = \text{base} \times \text{height}$
- $\text{Area} = 15 \times 8 = 120$ square meters

Problem 6: The area of a parallelogram is 180 square meters, and the base length is 12 meters. Find the height.

Solution:

- $\text{height} = \frac{\text{Area}}{\text{base}}$
- $\text{height} = \frac{180}{12} = 15$ meters

Problem 7: In a parallelogram, if the side length is 10 meters and the height is 6 meters, what is the area? (Assume the side length is the base.)

Solution:

- $\text{Area} = \text{base} \times \text{height} = 10 \times 6 = 60$ square meters

Complex Application Problems

- Using diagonals to find the area when height is unknown.
- Estimating land area from irregular measurements involving parallelogram-shaped plots.

Advanced Word Problems and Real-World Applications

Real-life scenarios often involve combining multiple shapes and dimensions, requiring critical thinking and multi-step calculations.

Examples of Complex Word Problems

Example 1: A rectangular garden measures 50 meters in length and 30 meters in width. A path of uniform width surrounds the garden, increasing its total area to 2,500 square meters. Find the width of the path.

Solution Approach:

- Let w be the width of the path.
- Total dimensions including the path: $(50 + 2w)$ and $(30 + 2w)$.
- Set up the equation: $(50 + 2w)(30 + 2w) = 2500$.
- Expand and solve the quadratic:

[

$$(50 + 2w)(30 + 2w) = 2500$$

]

[

$$1500 + 100w + 60w + 4w^2 = 2500$$

]

[

$$4w^2 + 160w + 1500 = 2500$$

]

[

$$4w^2 + 160w - 1000 = 0$$

]

- Divide through by 4:

\[

$$w^2 + 40w - 250 = 0$$

\]

- Use quadratic formula:

\[

$$w = \frac{-40 \pm \sqrt{40^2 - 4 \times 1 \times (-250)}}{2}$$

\]

\[

$$w = \frac{-40 \pm \sqrt{1600 + 1000}}{2} = \frac{-40 \pm \sqrt{2600}}{2}$$

\]

- Approximate:

\[

$$\sqrt{2600} \approx 50.99$$

\]

- Possible solutions:

\[

$$w = \frac{-40 + 50.99}{2} \approx \frac{10.99}{2} \approx 5.495$$

\]

\[

$$w = \frac{-40 - 50.99}{2} \approx \frac{-90.99}{2}$$

QuestionAnswer How do you find the area of a rectangle with length 8 meters and width 5 meters? Multiply the length by the width: $8 \times 5 = 40$ square meters. A square has a perimeter of 36 meters. What is its area? First, find the side length: $36 \div 4 = 9$ meters. Then, $\text{area} = 9 \times 9 = 81$ square meters. If the base of a parallelogram is 10 cm and the height is 7 cm, what is its area? $\text{Area} = \text{base} \times \text{height} = 10 \times 7 = 70$ square centimeters. A rectangle's length is twice its width. If the area is 48 square meters, what are the dimensions? Let width = w , then length = $2w$. $\text{Area} = w \times 2w = 2w^2 = 48$. So, $w^2 = 24$, $w \approx 4.9$ meters. Length ≈ 9.8 meters. How do you determine the area of a parallelogram given the diagonals and the angle between them? Use the formula: $\text{Area} = \frac{1}{2} \times d_1 \times d_2 \times \sin(\text{angle between diagonals})$. What is the area of a square with a diagonal length of $10\sqrt{2}$ cm? Diagonal = $s\sqrt{2}$, so $s = \text{diagonal} / \sqrt{2} = 10\sqrt{2} / \sqrt{2} = 10$ cm. $\text{Area} = s^2 = 10 \times 10 = 100$ square centimeters. A rectangle has a length of 15 meters and an area of 150 square meters. What is its width? $\text{Width} = \text{area} \div \text{length} = 150 \div 15 = 10$ meters. How do you find the area of a rhombus if you know the lengths of its diagonals? $\text{Area} = \frac{1}{2} \times d_1 \times d_2$, where d_1 and d_2 are the diagonals. In a parallelogram, if the base is 12 cm and the height is 9 cm, what is its area? $\text{Area} = \text{base} \times \text{height} = 12 \times 9 = 108$ square centimeters.

Related keywords: area calculation, perimeter, geometry, shape problems, algebra, rectangles, squares, parallelograms, formulas, math exercises

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